



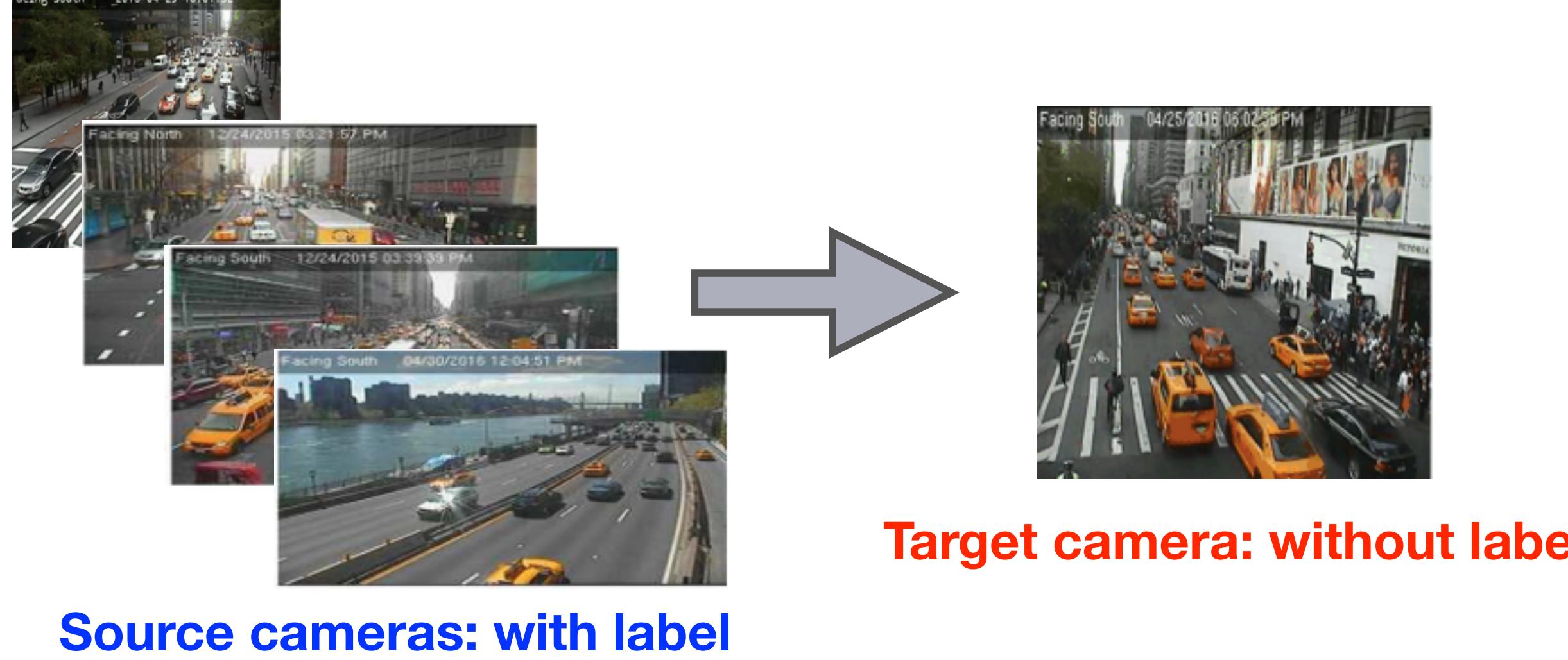
# Adversarial Multiple Source Domain Adaptation

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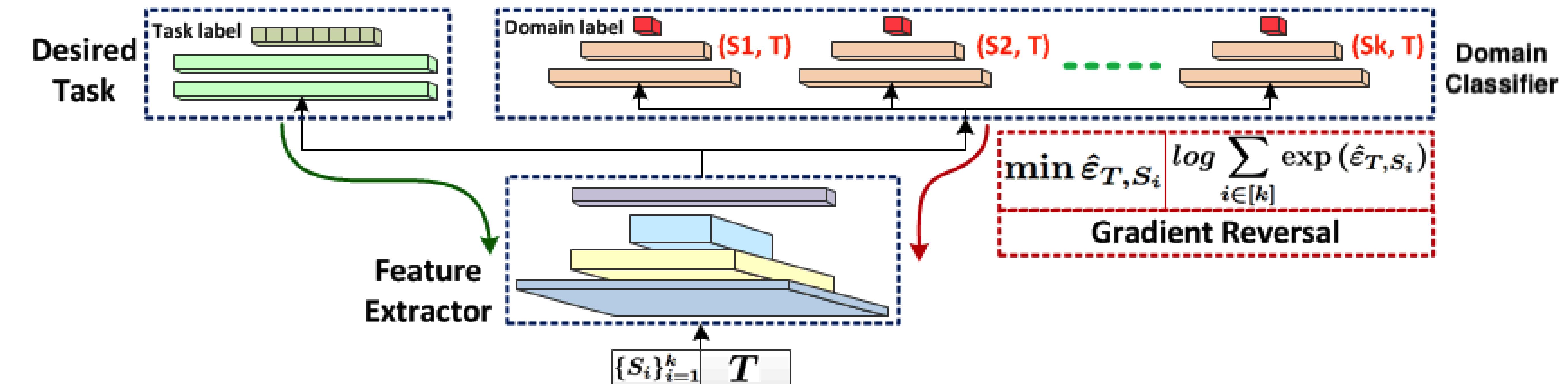


## Summary

Unsupervised Domain adaptation: **Source  $\neq$  Target**



## Models and Algorithms



**Theorem (informal):**  $\mathcal{H}$  is a hypothesis class and  $VCdim(\mathcal{H}) = d/Pdim(\mathcal{H}) = d$ .  $\widehat{\mathcal{D}}_T$  and  $\{\widehat{\mathcal{D}}_{S_i}\}_{i=1}^k$  are  $m$  samples generated from each domain. Define  $\widehat{\mathcal{H}} := \{\mathbb{I}_{|h(x)-h'(x)|>t} : h, h' \in \mathcal{H}, 0 \leq t \leq 1\}$  to be the set of threshold functions. Then for  $\forall \alpha \in \Delta^k$ , for  $\delta \in (0, 1)$ ,  $\forall h \in \mathcal{H}$ , w.p.  $\geq 1 - \delta$ :

Classification:

$$\varepsilon_T(h) \leq \sum_{i \in [k]} \alpha_i \left( \widehat{\varepsilon}_{S_i}(h) + \frac{1}{2} d_{\mathcal{H}\Delta\mathcal{H}}(\widehat{\mathcal{D}}_T; \widehat{\mathcal{D}}_{S_i}) \right) + \lambda_\alpha + \widetilde{O} \left( \sqrt{\frac{d \log(1/\delta)}{km}} \right), \quad \text{and} \quad \varepsilon_T(h) \leq \sum_{i \in [k]} \alpha_i \left( \widehat{\varepsilon}_{S_i}(h) + \frac{1}{2} d_{\mathcal{H}}(\widehat{\mathcal{D}}_T; \widehat{\mathcal{D}}_{S_i}) \right) + \lambda_\alpha + \widetilde{O} \left( \sqrt{\frac{d \log(1/\delta)}{km}} \right)$$

Regression:

## Preliminary

Given hypothesis class  $\mathcal{H}$  and  $\mathcal{A}_{\mathcal{H}} := \{h^{-1}(1) \mid h \in \mathcal{H}\}$ ,  $\mathcal{H}$ -divergence is:  $d_{\mathcal{H}}(\mathcal{D}, \mathcal{D}') := 2 \sup_{A \in \mathcal{A}_{\mathcal{H}}} |\Pr_{\mathcal{D}}(A) - \Pr_{\mathcal{D}'}(A)|$ . Generalization bound for single-source-single-target binary classification (Blitzer et al. NIPS' 08), using  $m$  instances, with probability  $\geq 1 - \delta$ ,  $\forall h \in \mathcal{H}$ :

$$\varepsilon_T(h) \leq \widehat{\varepsilon}_S(h) + \frac{1}{2} d_{\mathcal{H}\Delta\mathcal{H}}(\widehat{\mathcal{D}}_S, \widehat{\mathcal{D}}_T) + \lambda + O \left( \sqrt{\frac{d \log(m/d) + \log(1/\delta)}{m}} \right)$$

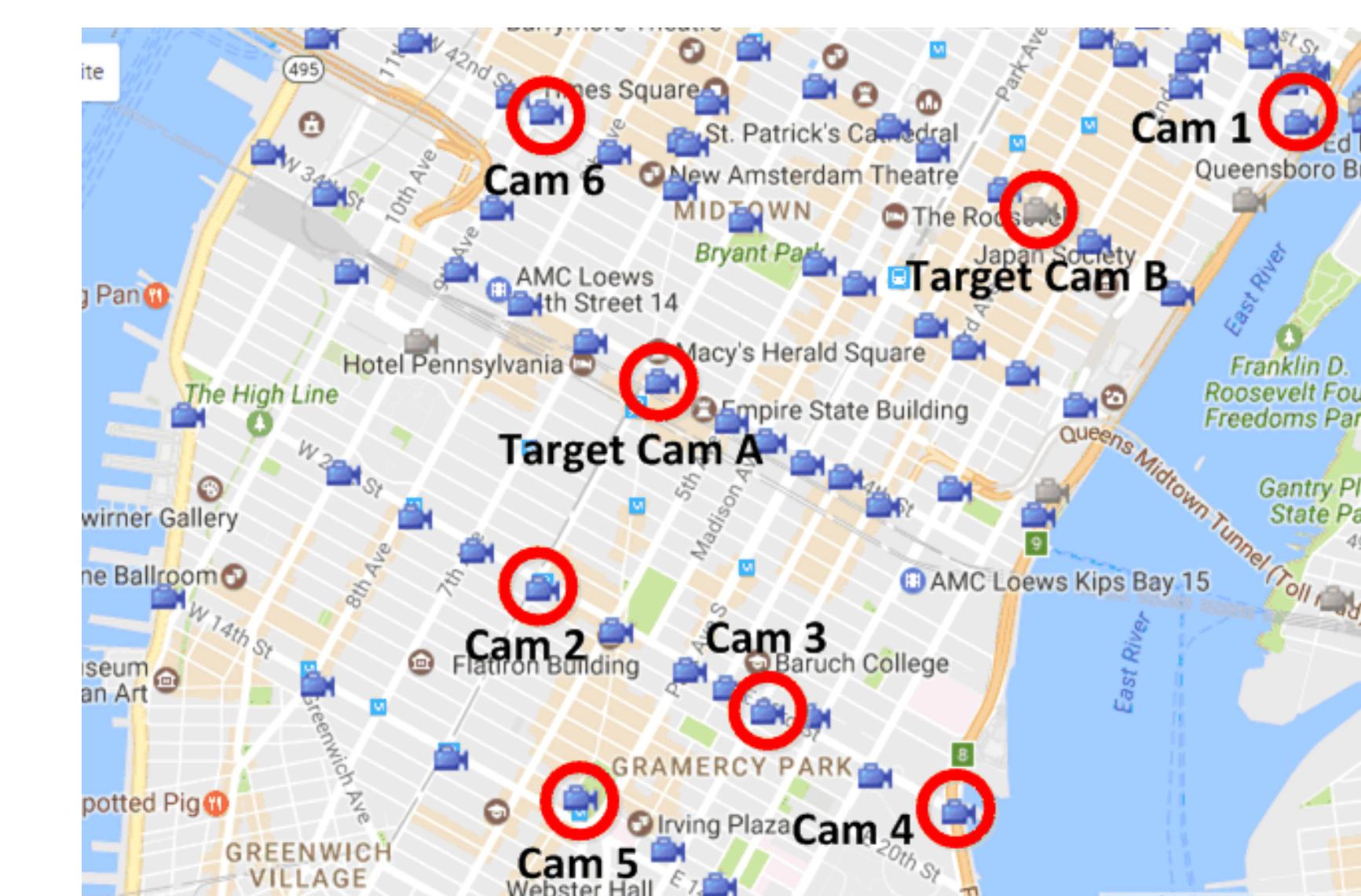
- $\widehat{\varepsilon}_S(h)/\varepsilon_T(h)$ : empirical/population source/target binary classification error.

- $d_{\mathcal{H}\Delta\mathcal{H}}(\widehat{\mathcal{D}}_S, \widehat{\mathcal{D}}_T)$ : empirical  $\mathcal{H}\Delta\mathcal{H}$ -divergence between source and target domains.
- $\lambda := \min_{h' \in \mathcal{H}} \varepsilon_S(h') + \varepsilon_T(h')$ .

A naive extension to  $k$  source domains with union bound:

$$\varepsilon_T(h) \leq \max_{i \in [k]} \left\{ \widehat{\varepsilon}_{S_i}(h) + \frac{1}{2} d_{\mathcal{H}\Delta\mathcal{H}}(\widehat{\mathcal{D}}_T; \widehat{\mathcal{D}}_{S_i}) + \lambda_i \right\} + O \left( \sqrt{\frac{1}{m} \left( \log \frac{k}{\delta} + d \log \frac{m}{d} \right)} \right)$$

## Datasets:



- WebCamT (Zhang et al, CVPR' 17), public dataset for vehicle counting. Image resolution:  $352 \times 240$ .
- 8 cameras. 6 as sources and each of the rest two as target. 2,000 images for each domain.

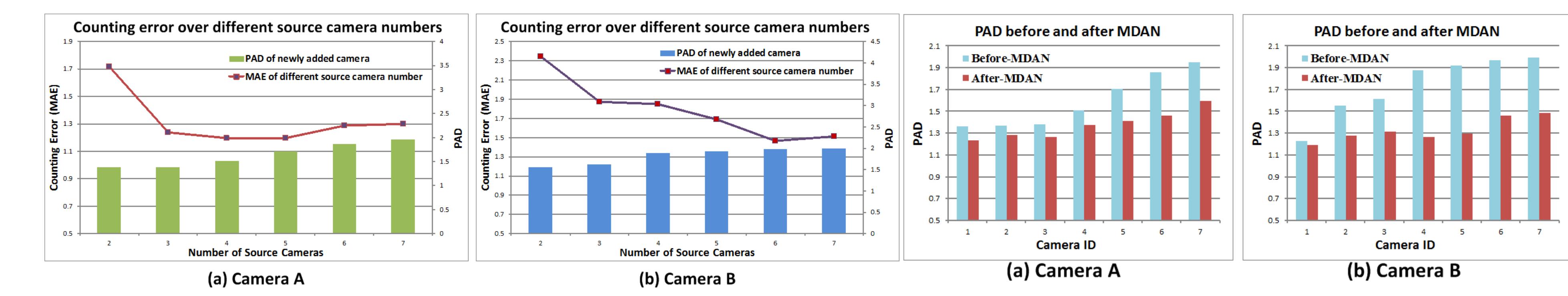
## Methods:

- FCN: Fully-convolutional NN, without domain adaptation.
- DANN: Combine all sources into one, with adversarial learning.

## Experiments

Table: Counting error statistics. S is the number of source cameras; T is the target camera id.

S	T	Ours		DANN	FCN	T	Ours		DANN	FCN
		Hard-Max	Soft-Max				Hard-Max	Soft-Max		
2	A	1.8101	<b>1.7140</b>	1.9490	1.9094	B	2.5059	<b>2.3438</b>	2.5218	2.6528
3	A	1.3276	<b>1.2363</b>	1.3683	1.5545	B	1.9092	<b>1.8680</b>	2.0122	2.4319
4	A	1.3868	<b>1.1965</b>	1.5520	1.5499	B	<b>1.7375</b>	1.8487	2.1856	2.2351
5	A	1.4021	<b>1.1942</b>	1.4156	1.7925	B	1.7758	<b>1.6016</b>	1.7228	2.0504
6	A	1.4359	<b>1.2877</b>	2.0298	1.7505	B	1.5912	<b>1.4644</b>	1.5484	2.2832
7	A	1.4381	<b>1.2984</b>	1.5426	1.7646	B	1.5989	<b>1.5126</b>	1.5397	1.7324



## Reference

- Blitzer et al., *Learning bounds for domain adaptation*, NIPS 2010.
- Zhang et al., *Understanding traffic density from large-scale web camera data*, CVPR 2017.